

The Crystal and Molecular Structure of Tricyclo[5,3,0,0^{2,6}]decane-4,9-dione, a Photochemical Product of Cyclodeca-3,8-diene-1,6-dione

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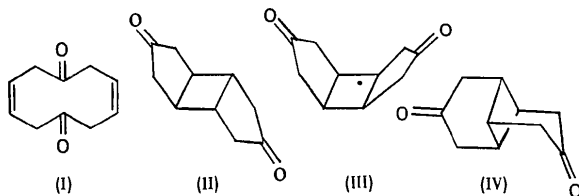
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Irradiation of *cis,cis*-cyclodeca-3,8-diene-1,6-dione leads to a tricyclic *anti* product C₁₀H₁₂O₂. Crystals are orthorhombic, space group *Pbca*, with $a=10.852(4)$, $b=13.086(4)$, and $c=11.739(5)$ Å, $Z=8$. 1490 independent reflexions were measured on an automated diffractometer with graphite-monochromated Mo $K\alpha$ radiation. The structure was solved by direct methods and refined by block-diagonal and full-matrix least-squares methods to $R=0.046$. The non-planar cyclobutane ring has a dihedral angle of 163.1° , and the two C–C bonds in this ring not involved in ring fusion are significantly shorter ($1.546, 1.542$ Å) than in similar compounds.

Introduction

Chemical analysis suggested that the irradiation of a solution of *cis,cis*-cyclodeca-3,8-diene-1,6-dione (I) leads to the *anti* tricyclo[5,3,0,0^{2,6}]dione (II) rather than the *syn* (III) or the cross-bonded (IV) (Shani, 1968, 1972).



However, some unusual chemical properties and a non-zero dipole moment (Shani & Ta-Shma, 1974) raised doubts as to the correctness of this assignment. Since the discrepancy could not be resolved on the basis of preliminary space-group assignment and cell constants, a full structure determination was carried out.

Experimental

Crystals from material provided by Dr A. Shani were obtained by slow evaporation of an ether solution at *ca.* 5°C. Weissenberg and precession photographs indicated orthorhombic symmetry with systematic absences characteristic of space group *Pbca*: $0kl, k$ odd; $h0l, l$ odd; $hk0, h$ odd. Lattice constants were obtained from a least-squares fit of 15 reflexions with 2θ values ranging between 8 and 36° (Mo $K\alpha$).

Intensities were measured on a Syntex *P1* automated diffractometer with graphite-monochromated Mo radiation. 1490 reflexions for which $2\theta \leq 50.0^\circ$ were measured by a $\theta:2\theta$ scan. After Lorentz and polarization corrections, 412 reflexions had $F_o \leq 2.5\sigma(F_o)$ and were considered unobserved.

Crystal data

C₁₀H₁₂O₂
Orthorhombic
Space group *Pbca*

F.W. 164.2
 $\rho_{\text{calc}} = 1.31 \text{ g cm}^{-3}$
 $\rho_{\text{meas}} = 1.29 \text{ g cm}^{-3}$
(flotation, CCl₄-isooctane)

Table 1. Final positional and thermal parameters for non-hydrogen ($\times 10^4$) and hydrogen ($\times 10^3$) atoms

E.s.d.'s in parentheses are in units of the least significant digit. Hydrogen atoms are numbered according to the atoms to which they are bonded. Anisotropic thermal parameters are in the form $\exp[-2\pi^2 \sum_i \sum_j a_i a_j h_i h_j u^{ij}]$; isotropic, $\exp[-8\pi^2 \sin^2 \theta / \lambda^2]$.

	<i>x</i>	<i>y</i>	<i>z</i>	u^{11}	u^{22}	u^{33}	u^{12}	u^{23}	u^{13}
C(1)	1993 (2)	1360 ⁻ (2)	-614 [‡] (2)	399 (12)	392 [‡] (12)	449 ⁻ (12)	-3 (10)	40 (10)	-14 (10)
C(2)	3351 (2)	975 (2)	-632 (2)	383 (13)	503 (12)	484 ⁻ (13)	-31 (10)	0 (11)	78 (10)
C(3)	2000 (2)	1281 (2)	699 (2)	394 (12)	429 (13)	443 (12)	-45 (10)	17 (10)	38 (10)
C(4)	3423 (2)	1136 (2)	667 (2)	402 (13)	464 (13)	465 (13)	55 (10)	20 (10)	-34 (10)
C(5)	1219 (2)	586 (2)	-1244 (2)	457 (14)	562 (14)	517 (16)	-57 (11)	-15 (11)	-29 (11)
C(6)	1959 (2)	-382 (2)	-1231 (2)	711 (16)	466 (13)	407 (13)	-87 (12)	-53 (10)	32 (11)
C(7)	3288 (2)	-129 (2)	-1032 (3)	610 (16)	613 (16)	592 (16)	128 (13)	-112 (14)	34 (14)
C(8)	1734 (2)	2243 (2)	1364 (2)	448 (14)	591 (13)	507 (13)	54 (11)	-81 (10)	24 (10)
C(9)	2907 (2)	2848 (2)	1343 (2)	574 (13)	484 (15)	364 (17)	-52 (12)	-10 (13)	6 (12)
C(10)	3961 (2)	2153 (2)	1048 (3)	409 (17)	648 (12)	632 (14)	-84 (10)	-77 (9)	-31 (11)
O(6)	1546 (2)	-1230 (1)	-1371 (2)	1061 (14)	508 (14)	840 (16)	-152 (11)	-107 (12)	-51 (11)
O(9)	3002 (2)	3750 (1)	1543 (2)	971 (15)	496 (11)	805 (13)	-121 (10)	-135 (8)	140 (11)

Table 1 (cont.)

	x	y	z	μ^{150}
H(C1)	189 (2)	208 (2)	-87 (2)	25 (7)
H(C2)	390 (2)	137 (1)	-107 (2)	25 (7)
H(C3)	156 (2)	68 (1)	95 (2)	19 (7)
H(C4)	377 (2)	54 (1)	108 (2)	25 (7)
H(C5)	108 (2)	80 (2)	-204 (2)	37 (8)
H'(C5)	41 (2)	49 (1)	-93 (2)	28 (7)
H(C7)	363 (2)	-60 (2)	-50 (2)	43 (9)
H'(C7)	375 (3)	-17 (2)	-172 (2)	52 (9)
H(C8)	156 (2)	208 (2)	215 (2)	50 (9)
H'(C8)	108 (2)	266 (1)	105 (2)	29 (7)
H(C10)	445 (2)	247 (2)	46 (2)	43 (8)
H'(C10)	449 (2)	208 (2)	170 (2)	60 (10)

$a = 10.852(4) \text{ \AA}$ $Z = 8$
 $b = 13.086(4)$ $F(000) = 704$
 $c = 11.739(5)$ $\mu = 0.972 \text{ cm}^{-1} (\text{Mo K}\alpha)$
 $\lambda(\text{Mo K}\alpha) = 0.70926 \text{ \AA}$

Structure determination and refinement

The structure was solved with the program *MULTAN*. All 12 heavy atoms appeared in the *E* map corre-

sponding to the model with the highest figure of merit and the lowest residual (Germain, Main & Woolfson, 1971).

Least-squares refinement of the heavy atoms proceeded smoothly through three cycles (full-matrix) with isotropic temperature factors ($\sin \theta/\lambda \leq 0.30$), and three cycles (full-matrix) with anisotropic temperature factors ($\sin \theta/\lambda \leq 0.45$). Expected hydrogen atom positions were calculated from geometrical considerations and were included in the next two cycles with individual isotropic temperature factors; to save computer time the molecule was divided into three blocks. One final cycle of full-matrix refinement resulted in values for *R* of 0.046 (0.052 including 'unobserveds') and *R'* of 0.011. The function minimized was $\sum w(|kF_o|^2 - |F_c|^2)^2$ where *w* is $1.0/\sigma^2(F_o^2)$. Scattering factors were taken from *International Tables for X-ray Crystallography* (1965). The least-squares program used is a local version of *ORFLS* (Busing, Martin & Levy, 1963). Final positional parameters and temperature factors are given in Table 1, and observed and calculated structure factors in Table 2.

Table 2. Observed and calculated structure factors

The three columns list respectively *l*, $10kF_o$ and $10F_c$. *U* signifies reflexions for which $F_o \leq 2.5 \sigma(F_o)$. Asterisks indicate reflexions not included in least-squares refinement.

h	k	l	$10kF_o$	$10F_c$	U
0	0	0	0	0	
0	0	1	100	100	
0	0	2	200	200	
0	0	3	300	300	
0	0	4	400	400	
0	0	5	500	500	
0	0	6	600	600	
0	0	7	700	700	
0	0	8	800	800	
0	0	9	900	900	
0	0	10	1000	1000	
0	0	11	1100	1100	
0	0	12	1200	1200	
0	0	13	1300	1300	
0	0	14	1400	1400	
0	0	15	1500	1500	
0	0	16	1600	1600	
0	0	17	1700	1700	
0	0	18	1800	1800	
0	0	19	1900	1900	
0	0	20	2000	2000	
0	0	21	2100	2100	
0	0	22	2200	2200	
0	0	23	2300	2300	
0	0	24	2400	2400	
0	0	25	2500	2500	
0	0	26	2600	2600	
0	0	27	2700	2700	
0	0	28	2800	2800	
0	0	29	2900	2900	
0	0	30	3000	3000	
0	0	31	3100	3100	
0	0	32	3200	3200	
0	0	33	3300	3300	
0	0	34	3400	3400	
0	0	35	3500	3500	
0	0	36	3600	3600	
0	0	37	3700	3700	
0	0	38	3800	3800	
0	0	39	3900	3900	
0	0	40	4000	4000	
0	0	41	4100	4100	
0	0	42	4200	4200	
0	0	43	4300	4300	
0	0	44	4400	4400	
0	0	45	4500	4500	
0	0	46	4600	4600	
0	0	47	4700	4700	
0	0	48	4800	4800	
0	0	49	4900	4900	
0	0	50	5000	5000	
0	0	51	5100	5100	
0	0	52	5200	5200	
0	0	53	5300	5300	
0	0	54	5400	5400	
0	0	55	5500	5500	
0	0	56	5600	5600	
0	0	57	5700	5700	
0	0	58	5800	5800	
0	0	59	5900	5900	
0	0	60	6000	6000	
0	0	61	6100	6100	
0	0	62	6200	6200	
0	0	63	6300	6300	
0	0	64	6400	6400	
0	0	65	6500	6500	
0	0	66	6600	6600	
0	0	67	6700	6700	
0	0	68	6800	6800	
0	0	69	6900	6900	
0	0	70	7000	7000	
0	0	71	7100	7100	
0	0	72	7200	7200	
0	0	73	7300	7300	
0	0	74	7400	7400	
0	0	75	7500	7500	
0	0	76	7600	7600	
0	0	77	7700	7700	
0	0	78	7800	7800	
0	0	79	7900	7900	
0	0	80	8000	8000	
0	0	81	8100	8100	
0	0	82	8200	8200	
0	0	83	8300	8300	
0	0	84	8400	8400	
0	0	85	8500	8500	
0	0	86	8600	8600	
0	0	87	8700	8700	
0	0	88	8800	8800	
0	0	89	8900	8900	
0	0	90	9000	9000	
0	0	91	9100	9100	
0	0	92	9200	9200	
0	0	93	9300	9300	
0	0	94	9400	9400	
0	0	95	9500	9500	
0	0	96	9600	9600	
0	0	97	9700	9700	
0	0	98	9800	9800	
0	0	99	9900	9900	
0	0	100	10000	10000	

Results and discussion

Bond lengths and angles for the heavy atoms are shown in Fig. 1. Those involving hydrogen atoms are all normal (average bond length 0.97 Å). All chemically equivalent bond lengths and angles agree to within three standard deviations save the non-carbonyl internal angles in the two cyclopentanone rings, where the discrepancies are probably due to differences in ring conformation (see below). C(1)–C(3) and C(2)–C(4) are normal for sp^3 – sp^3 hybridization which this system approximates but are considerably shorter than the equivalent bonds in the photodimers of cyclopentanone (1.59 Å) (Margulis, 1965) and its 3-phenyl derivative (1.579, 1.581 Å) (Shaw, Fratini & Adams, 1974).

The cyclobutane ring is folded about an axis through the transannular atoms with a dihedral angle of 163.1° ; this is the largest value observed to date for crystallographic site symmetry 1. All other features of the ring compare favourably with those of earlier studies (Shirrell & Williams, 1973).

Although the cyclopentanone rings are *anti* to each other in accordance with the chemical analysis, the folding of the cyclobutane ring precludes a molecular inversion centre and accounts for the non-zero dipole moment of the material. A further contribution to the dipole moment may come from the small but significant differences between chemically equivalent torsion angles in the cyclopentanone rings.

The best planes of the cyclopentanone rings make angles of 107 and 108° with the best plane of the cyclobutane ring, as would be expected from nearly tetrahedral hybridization of the latter, although strictly speaking none of these moieties is or would be expected to be planar. The folding of the cyclopentanone rings about the axes C(5)···C(7) and C(8)···C(10) is such that both oxygen atoms are *endo* to the cyclobutane ring. Both carbonyl groups, comprising three carbon atoms and the oxygen, are planar within 0.004 Å.

The crystal is composed of sheets of molecules nearly perpendicular to **a** (Fig. 2). The intra-sheet relationship of carbonyl groups suggests a predominance of dipole-dipole interactions in this region of the structure whereas regions between sheets are limited to contacts of the H···H type, only two of which are shorter than 2.6 Å, suggesting that van der Waals forces dominate here.

References

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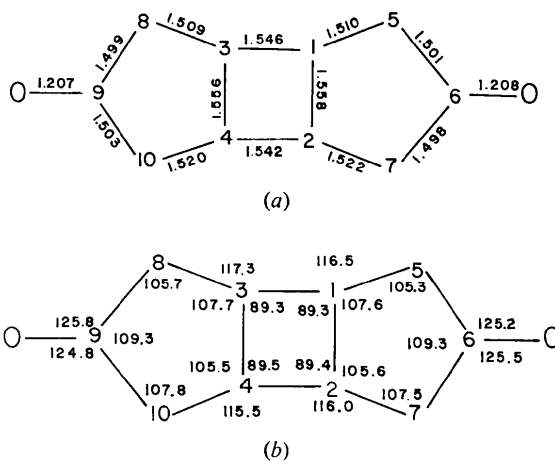


Fig. 1. Molecular dimensions for tricyclo[5,3,0,0^{2,6}]decane-4,9-dione. (a) Bond lengths (Å); average e.s.d. 0.003 Å. (b) Bond angles (°); average e.s.d. 0.2°.

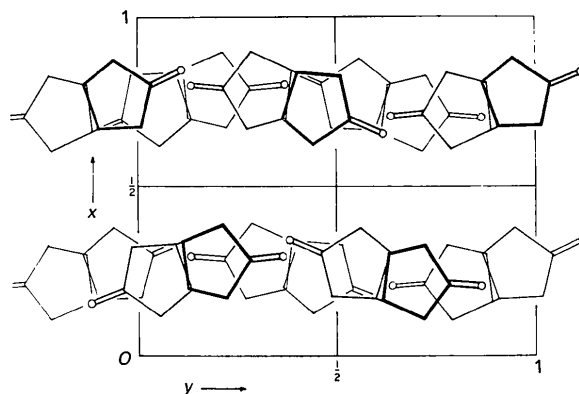


Fig. 2. View of the structure along the *c* axis.

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